

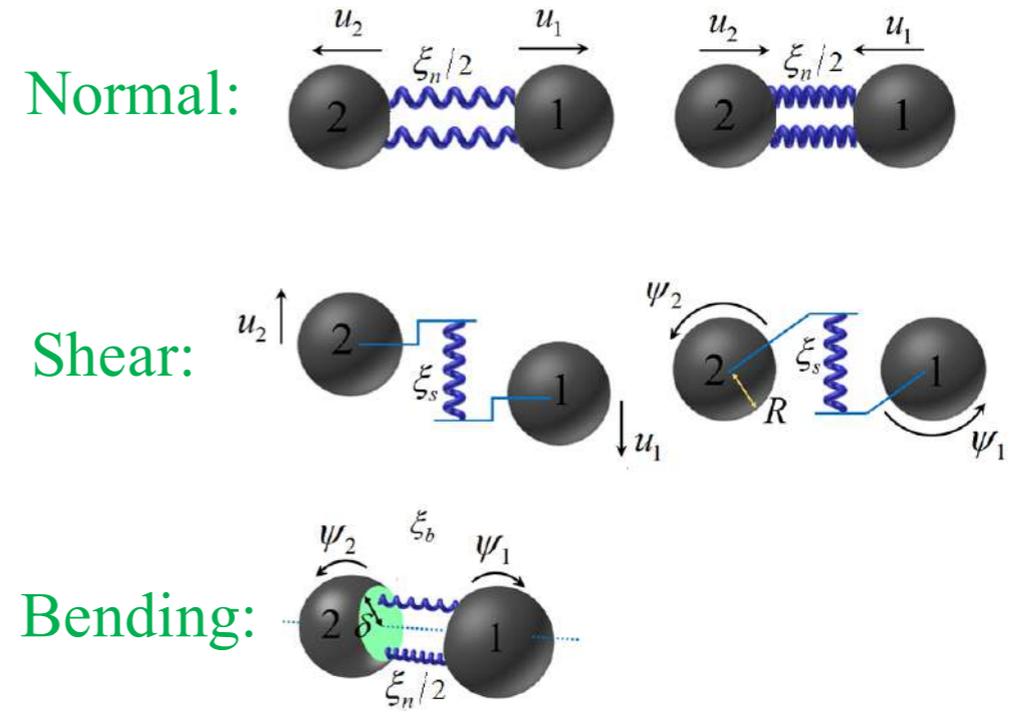
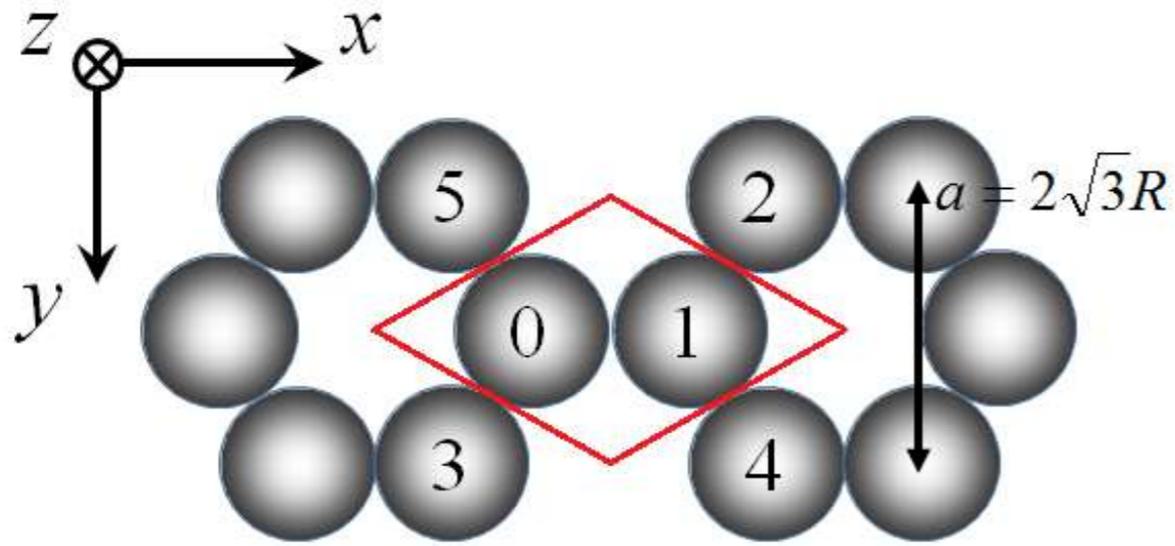


Phononics of Magneto-Granular Graphene: edge waves

Georgios Theocharis

in collaboration with F. Allein, L.-Y. Zheng, V. Tournat, V. Gusev
-Karystos-

Granular Graphene



Equations of motion:

$$M\ddot{u}_{xj} = \sum_i (\xi_n \Delta n_i \bar{e}_i + \xi_s \Delta s_i \bar{d}_i) \bar{e}_x$$

$$M\ddot{u}_{yj} = \sum_i (\xi_n \Delta n_i \bar{e}_i + \xi_s \Delta s_i \bar{d}_i) \bar{e}_y$$

$$I\ddot{\varphi}_j = R \sum_i (\xi_s \Delta s_i + \xi_b \Delta b_i)$$

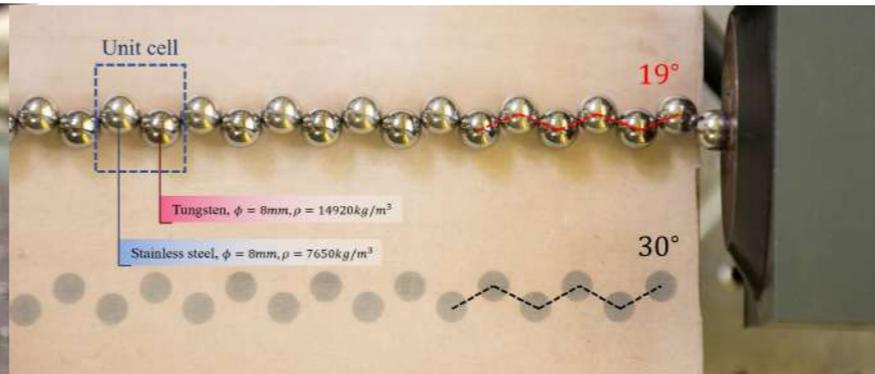
where i denotes the neighbor index. j is the sublattice index.

Magneto Granular crystals



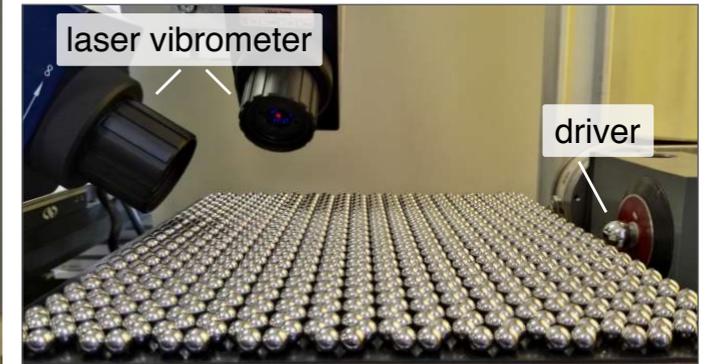
Monoatomic chain

F. Allein - LAUM 2016



Zig-zag chain

S. Qu, L.Zheng, F. Allein - LAUM 2019



2D Honeycomb

F. Allein - L.Zheng -LAUM 2018

Experimental setup:

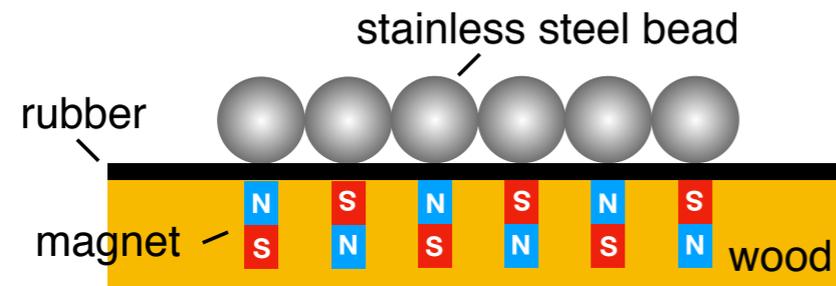
Periodic arrangements of elastic particles in contact under properly designed external magnetic fields, free of mechanical borders.

- Dynamics can range from near linear to highly nonlinear.
- **Rotational degrees of freedom** play an important role

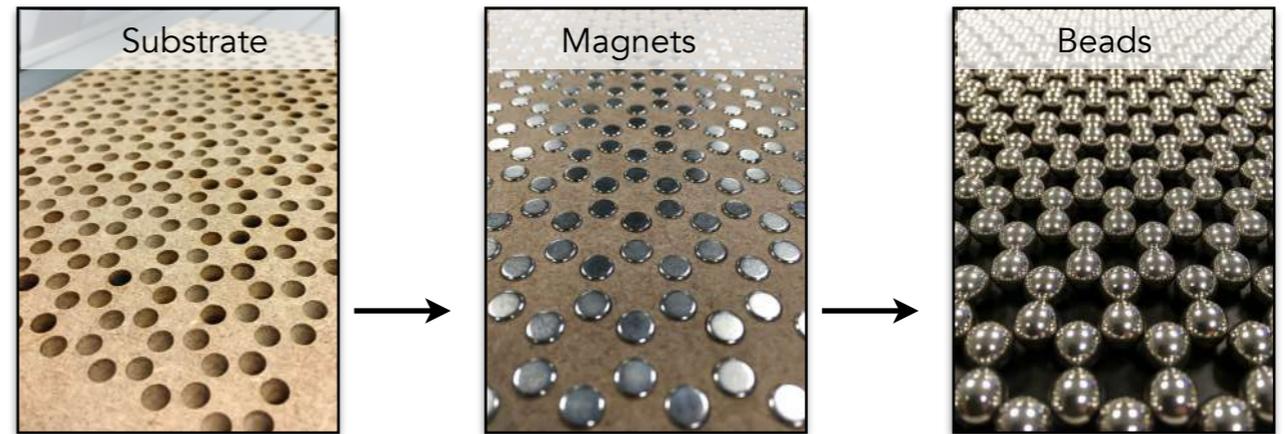
Granular crystals: Condensed Matter Physics meets materials

two other, overestimated features:
(in most of the studies, RDF have been ignored)

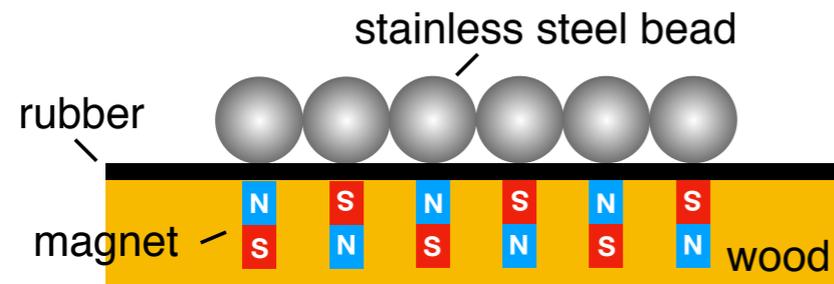
Magneto-Granular Graphene



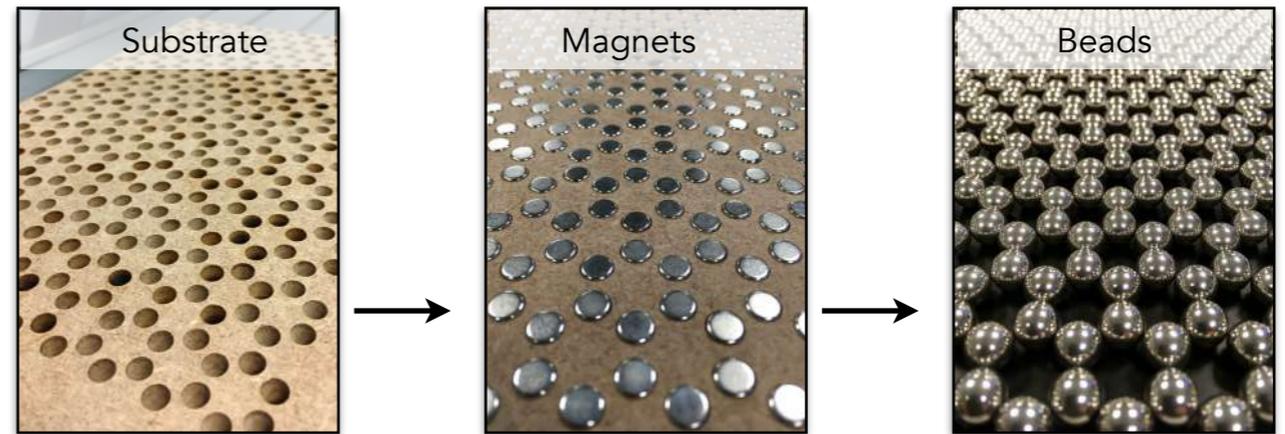
Diameter of bead: 8 mm



Magneto-Granular Graphene

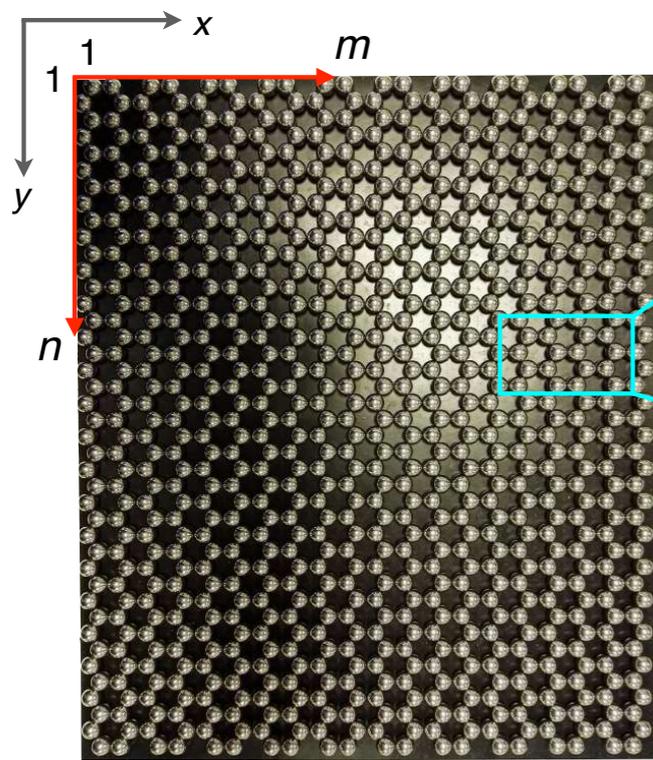


Diameter of bead: 8 mm

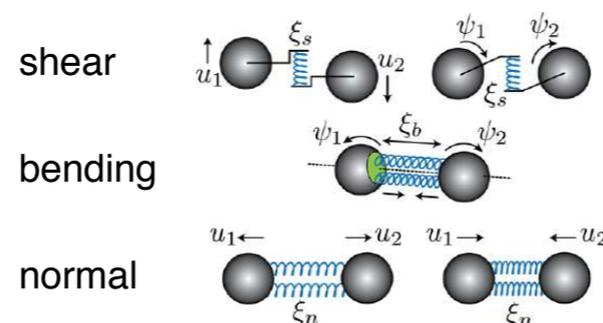
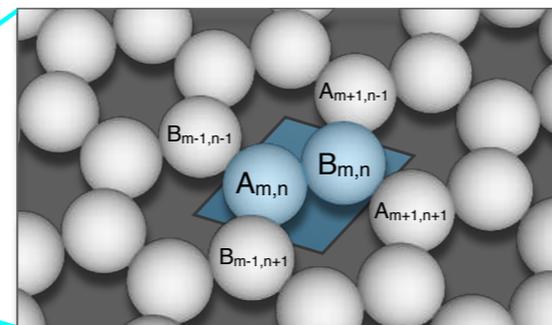


Precompression estimated: $F_0 = 1.5 \text{ N}$

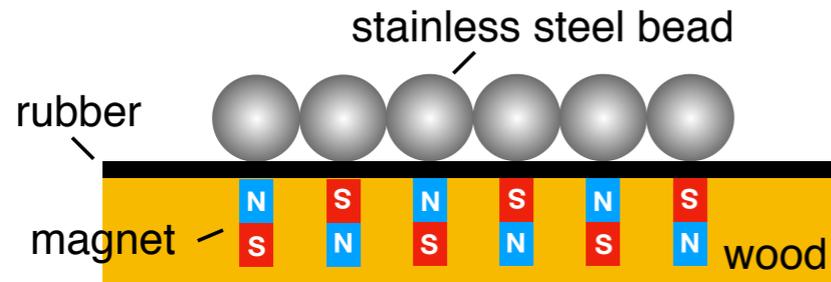
<https://www.instagram.com/p/BpbqY5dFQyn/>



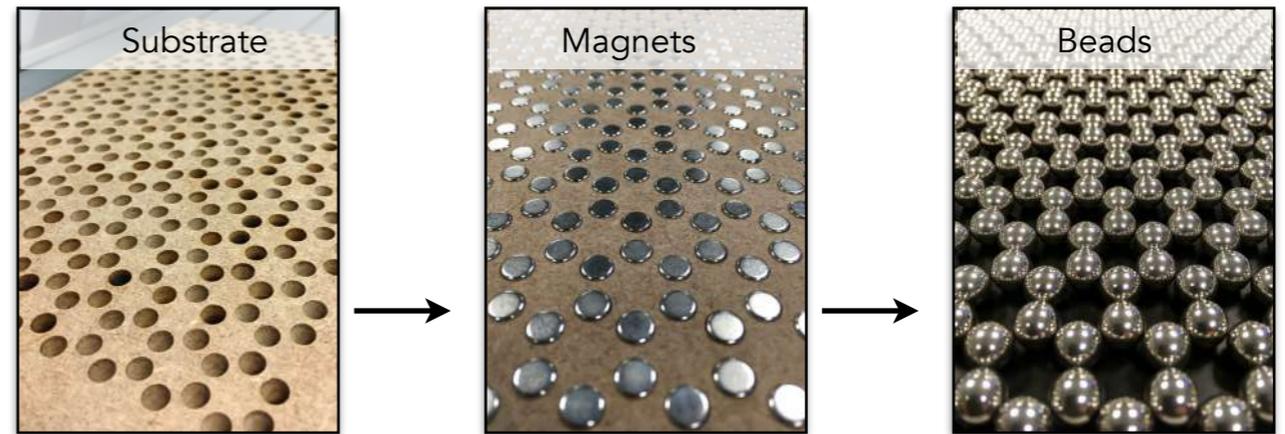
820 particles



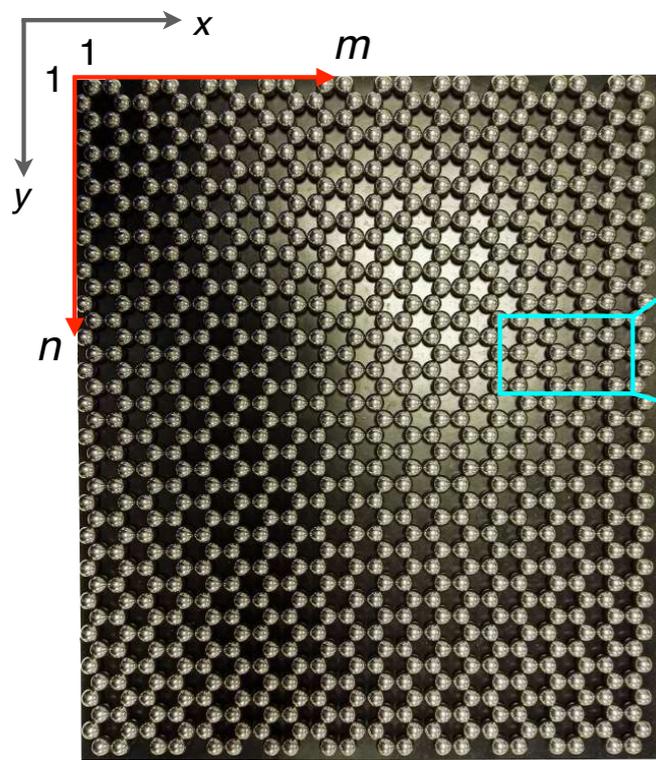
Magneto-Granular Graphene



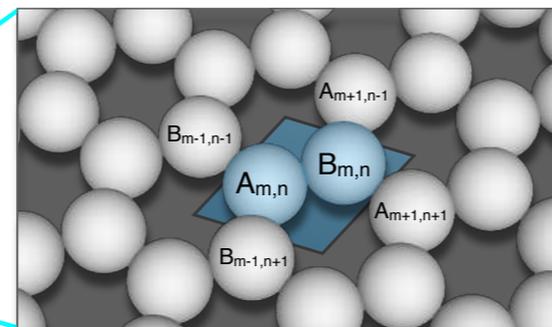
Diameter of bead: 8 mm



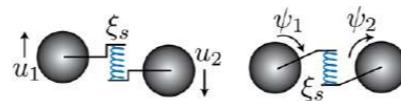
Precompression estimated: $F_0 = 1.5 \text{ N}$



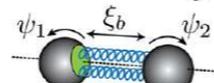
820 particles



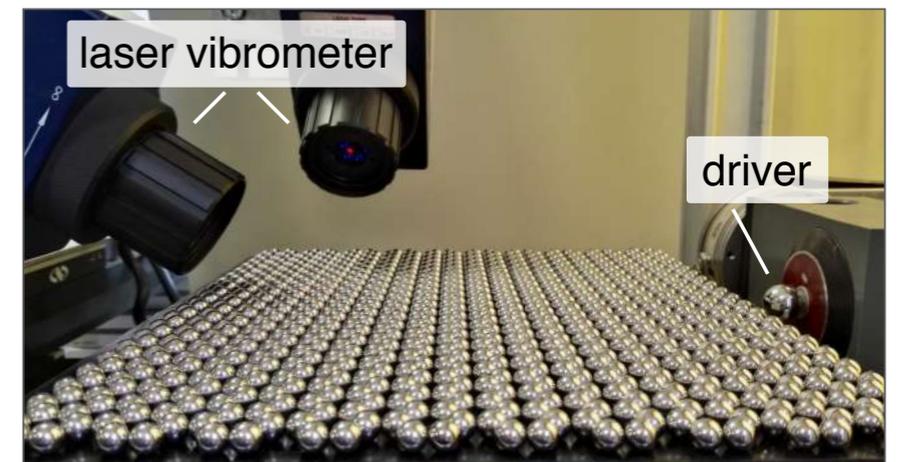
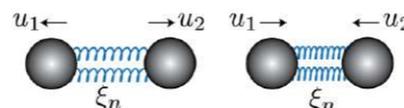
shear



bending

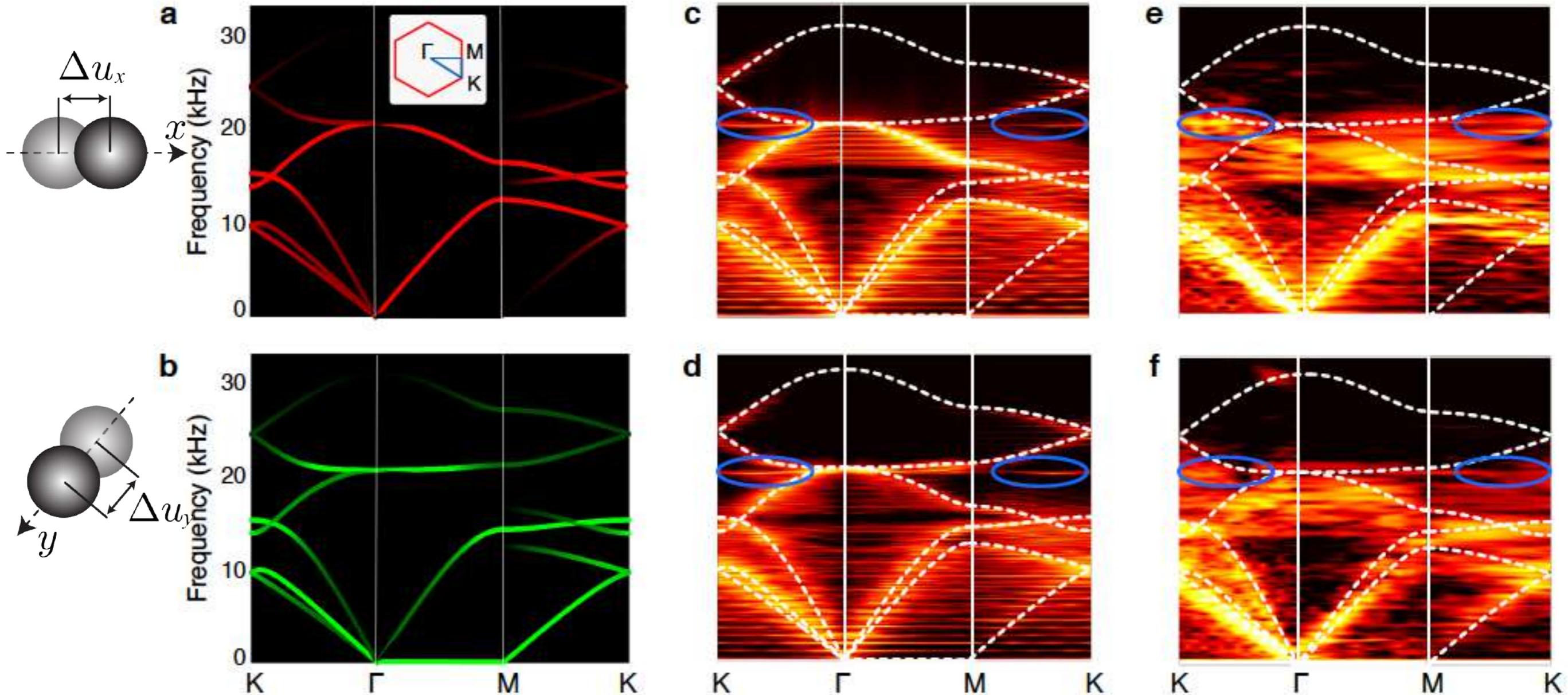
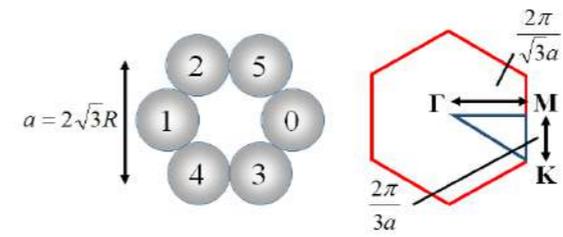


normal

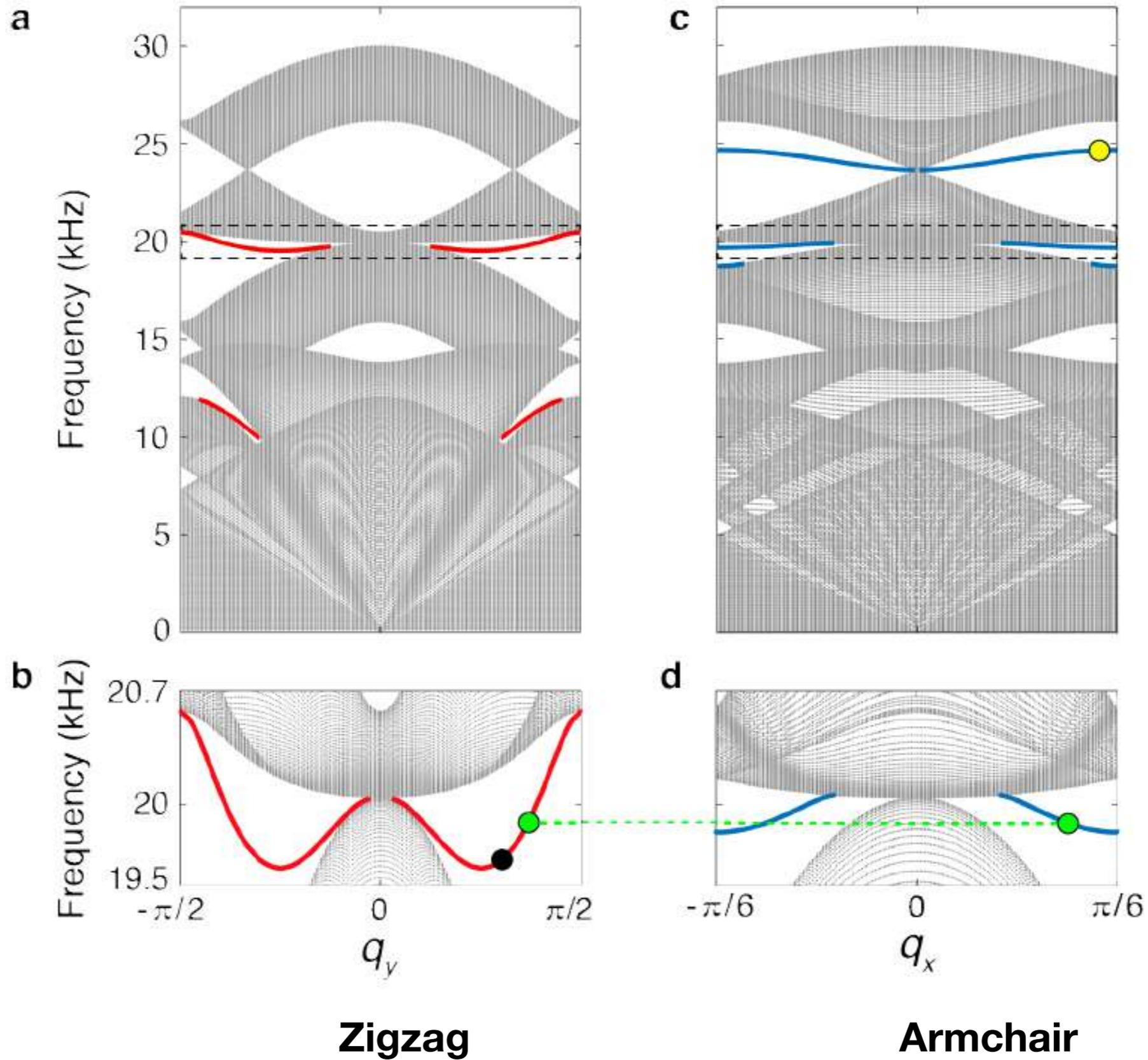


Magneto-Granular Graphene

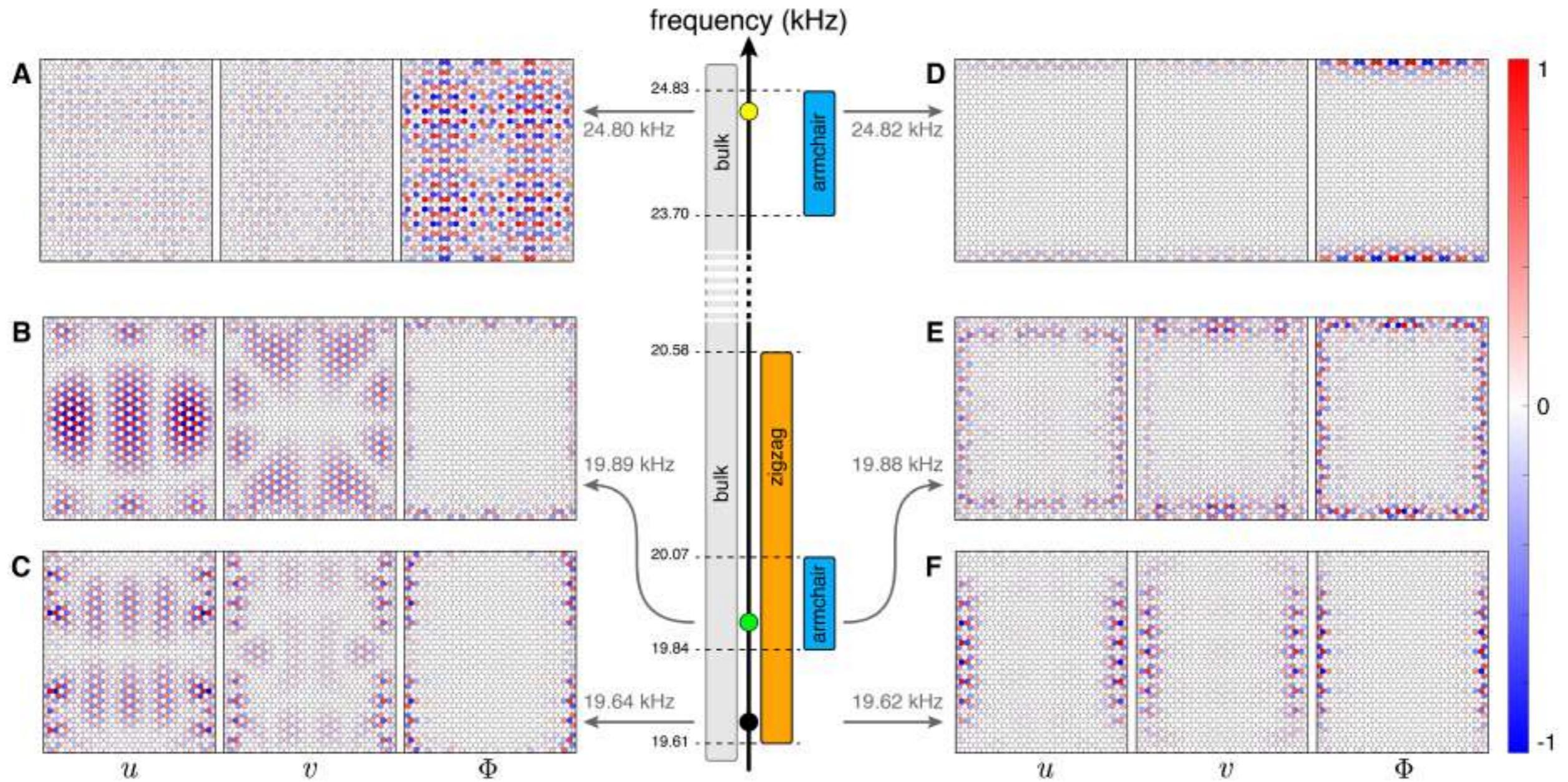
Dispersion curves:



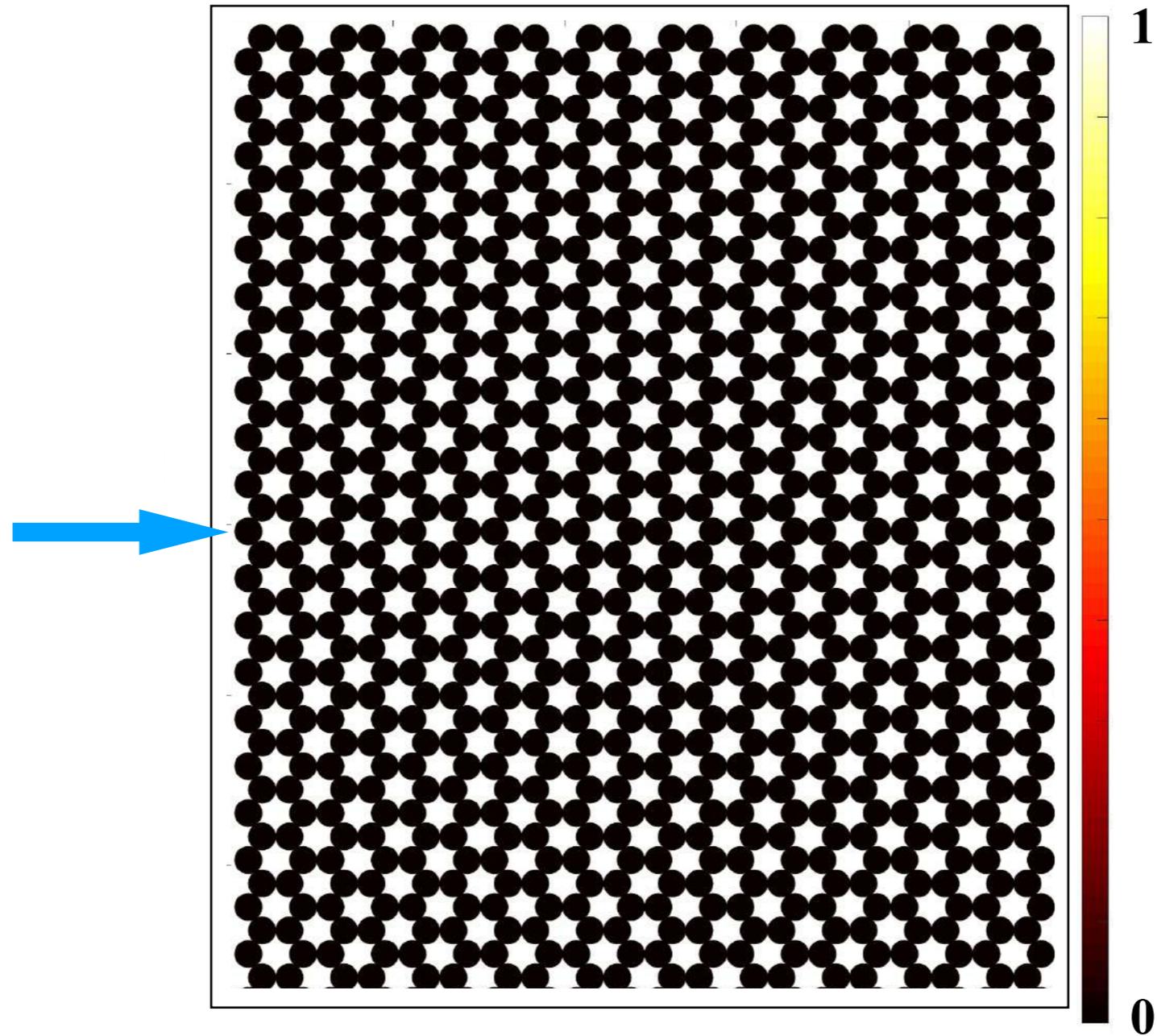
Edge Waves



Edge Waves

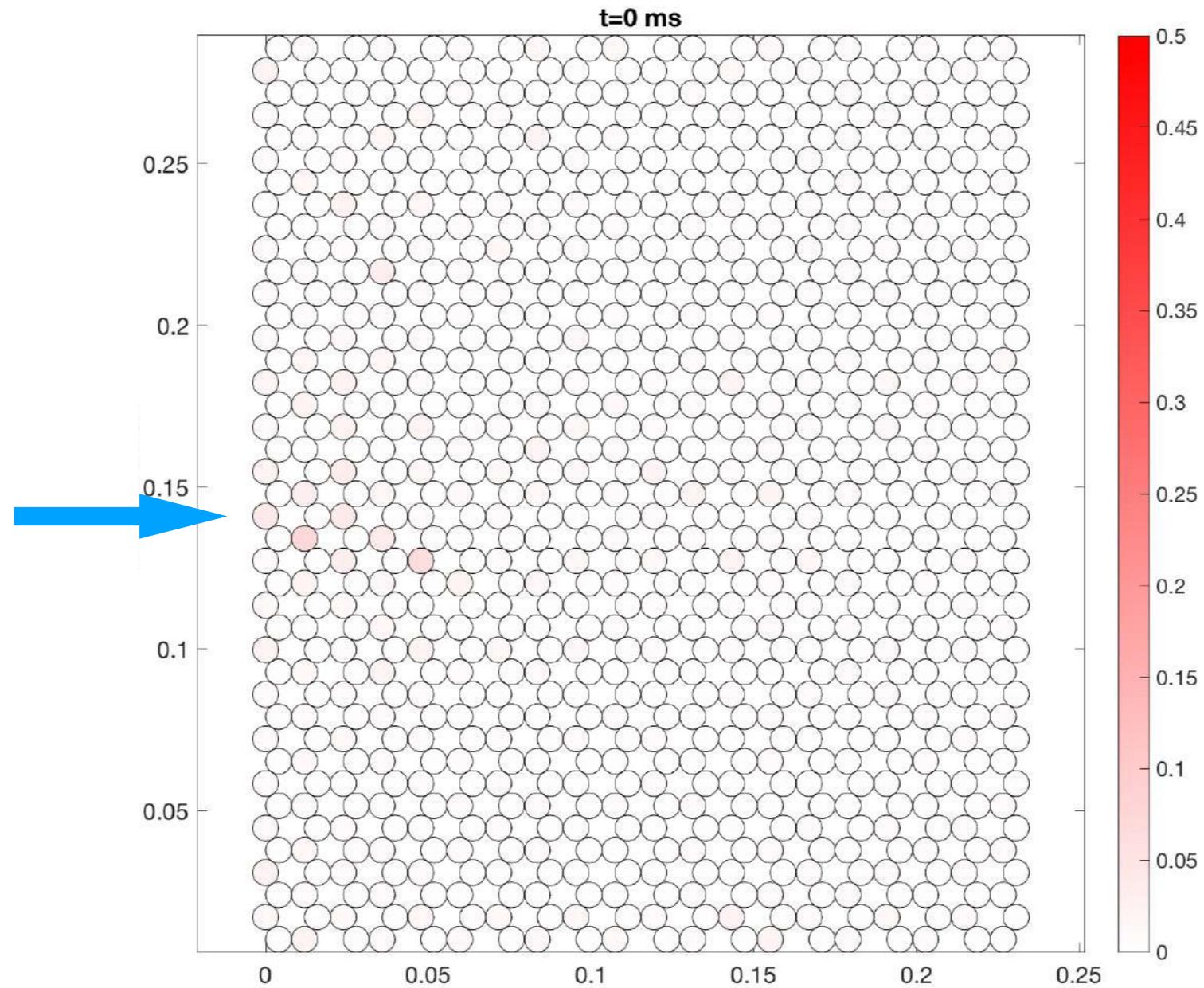


Numerical Simulation



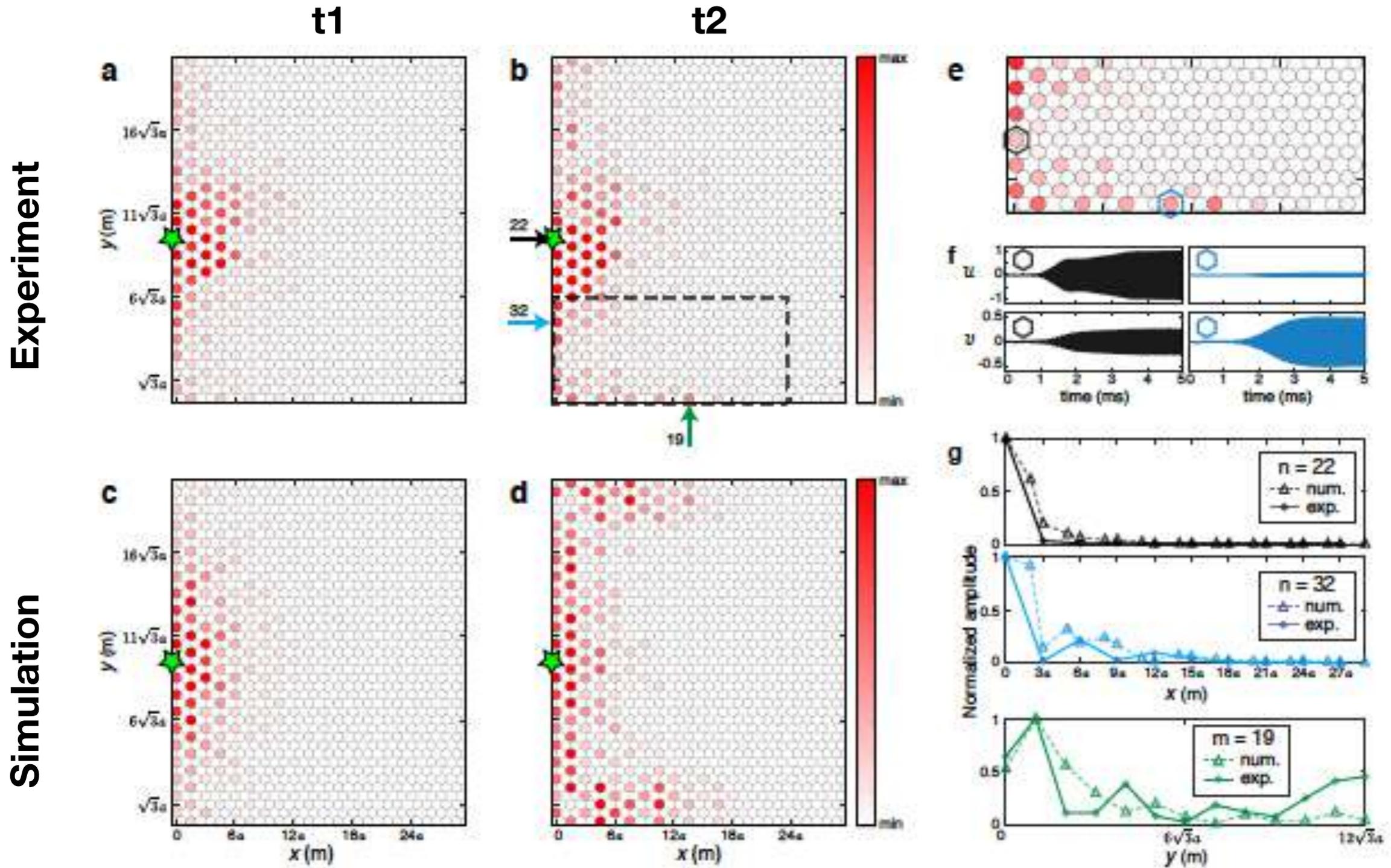
Harmonic excitation at 20 kHz

Experimental Observation



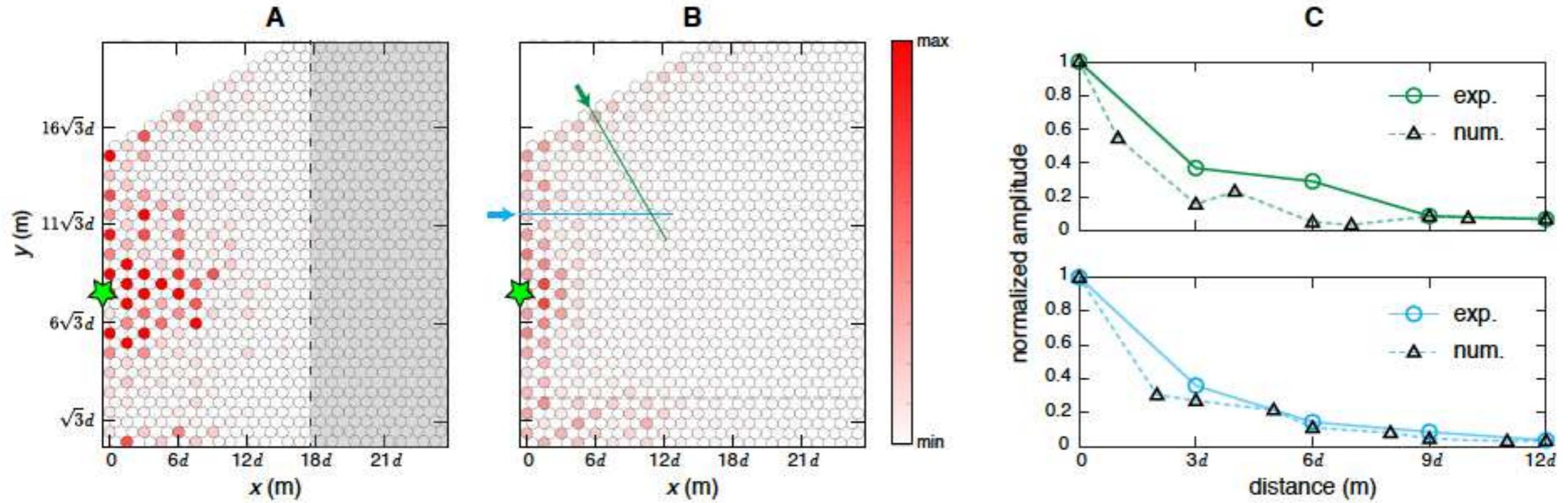
Harmonic excitation at 20 kHz

Edge Waves - Turning

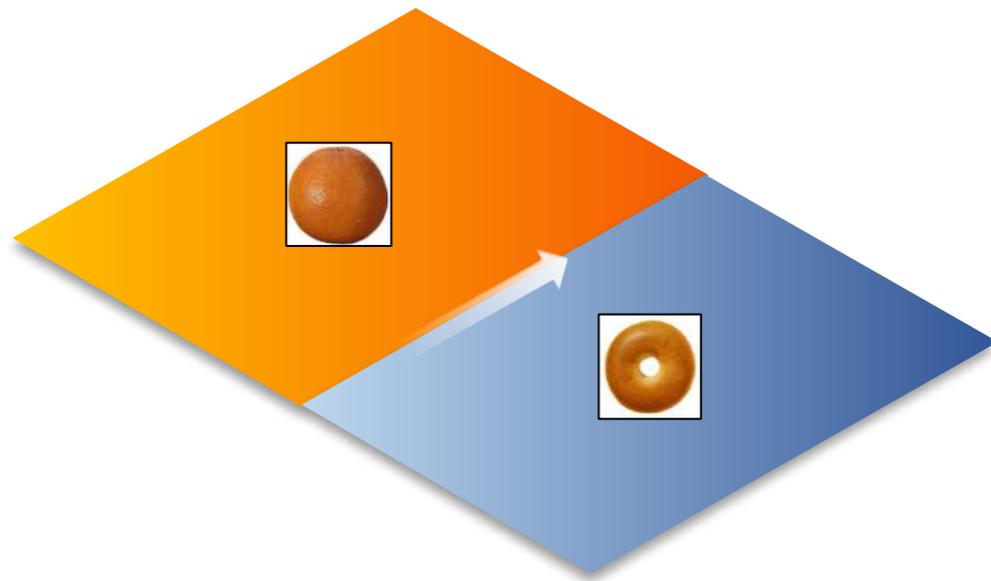


- L-Y Zheng, F; Allein, V. Tournat, V. Gusev, G. Theocharis, Granular Graphene: Direct observation of edge states in zigzag and armchair boundaries, **PRB 99, 184113 (2019)**

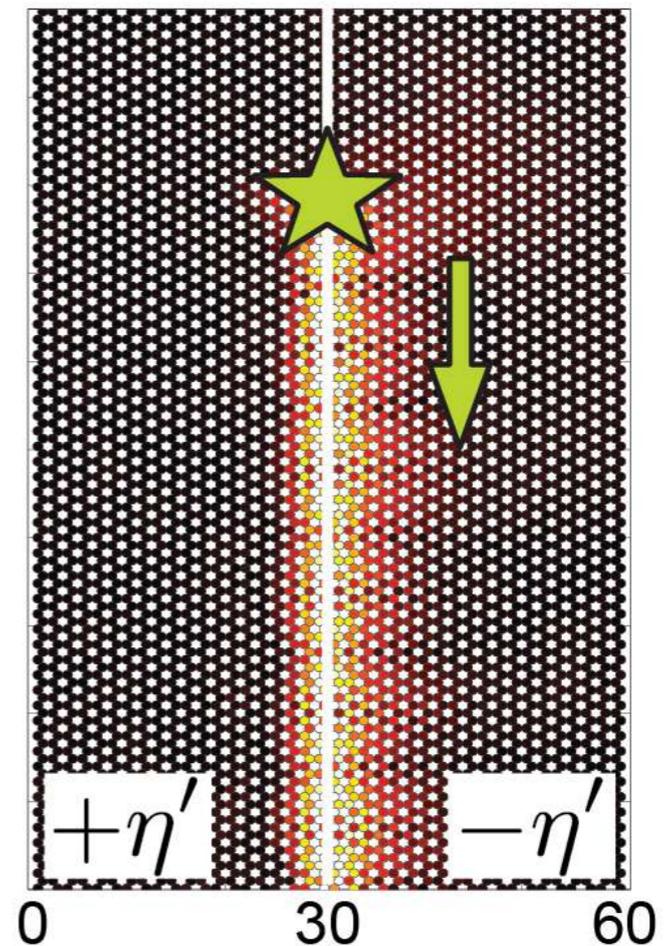
Edge Waves - Turning



Robust Transfer/ Waveguiding of Modes

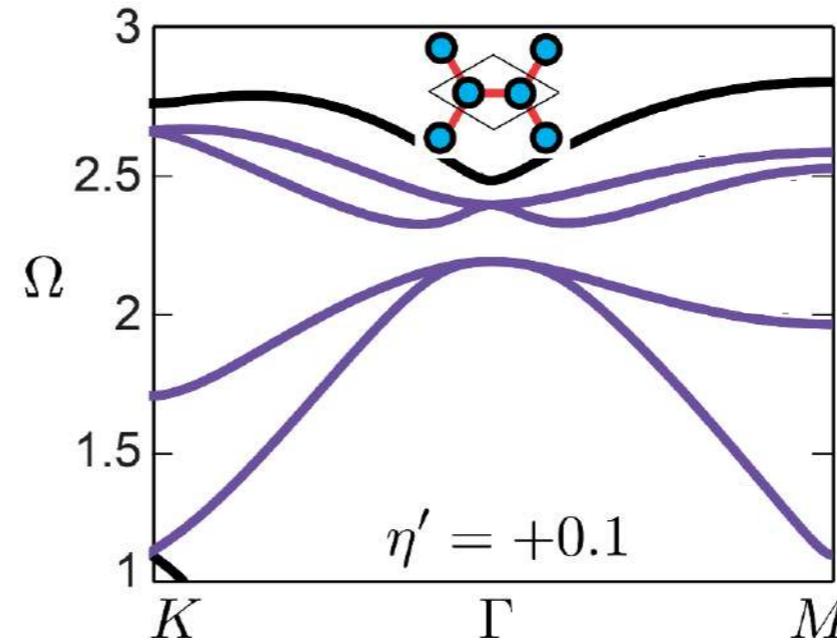
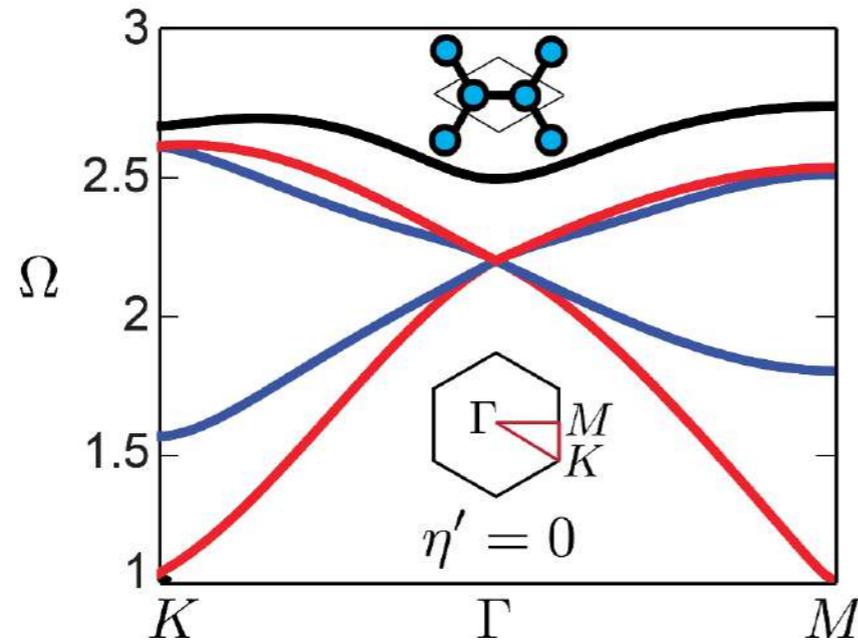


Topologically *distinct* structures



Topological Granular Graphene: mechanical analogue of Quantum Spin Hall effect

Topological Granular Graphene



Hamiltonian around Γ point:

$$H = V_D \vec{\sigma} \cdot \Delta \vec{k}$$

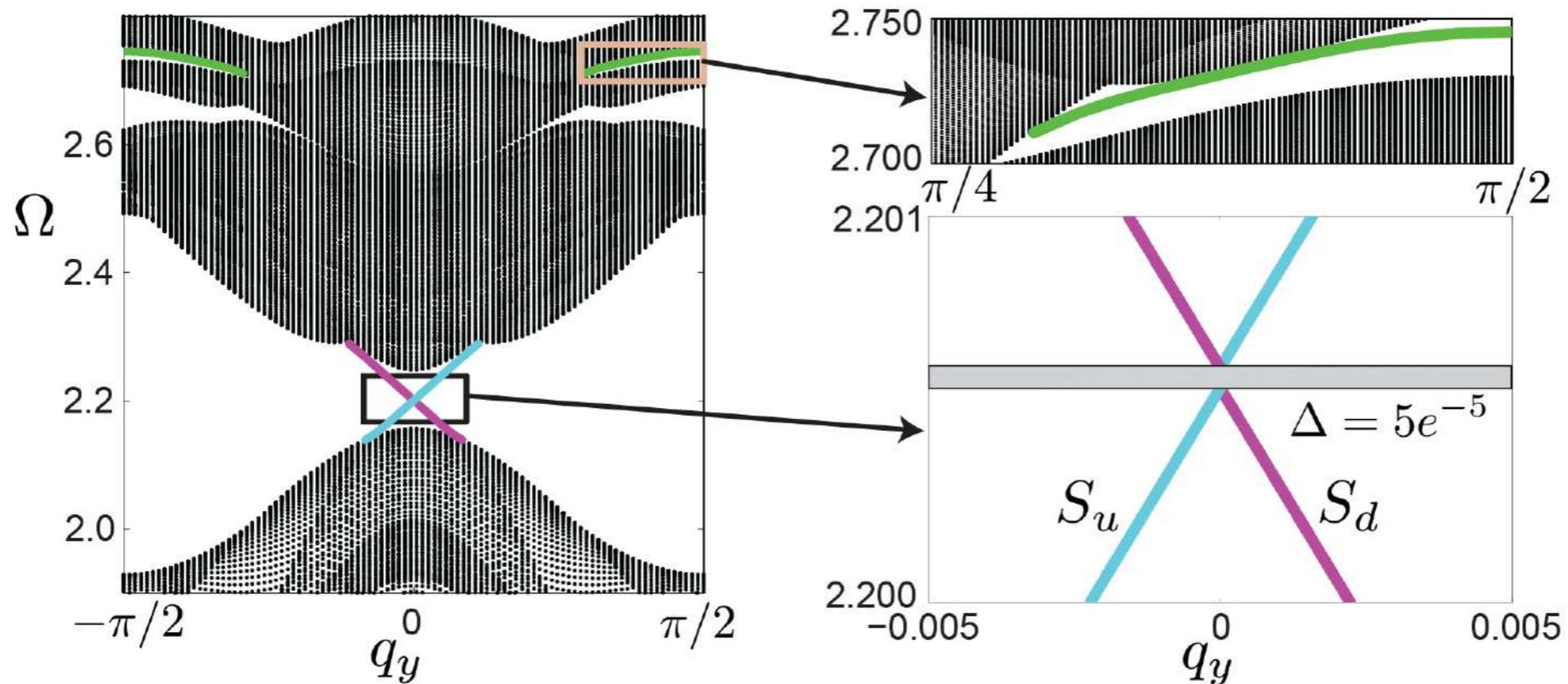
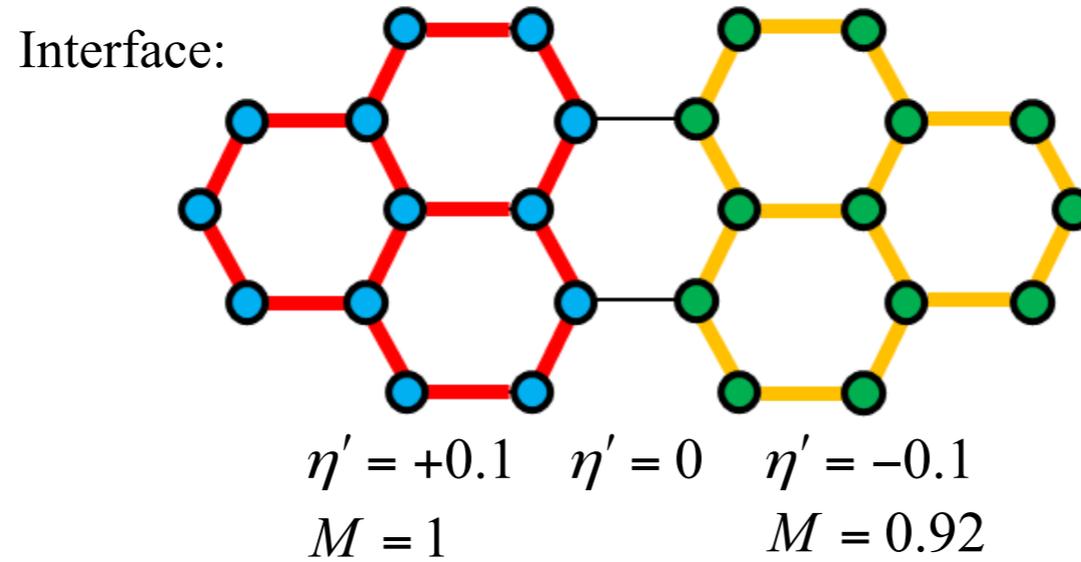


$$H_{\pm} = V_D \vec{\sigma} \cdot \Delta \vec{k} \pm m \sigma_z$$

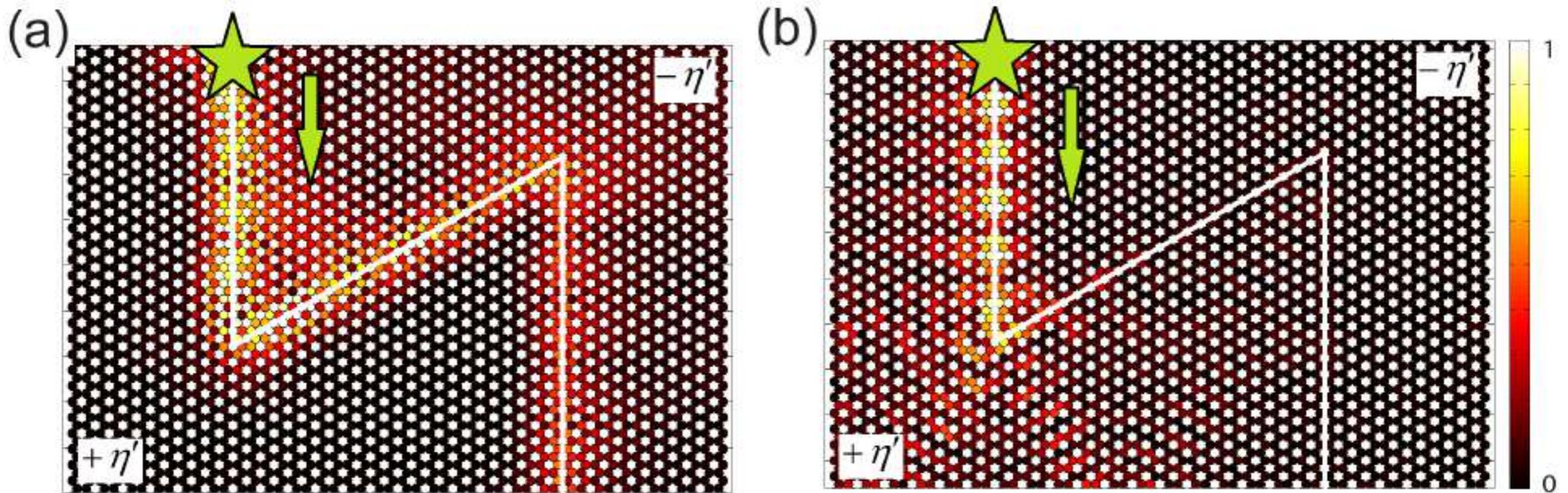
Double Dirac Cone by fine tuning of the stiffnesses

Mechanical Analogue of Quantum Spin Hall effect

Topological Granular Graphene



Topological Granular Mechanical Insulators



- L-Y Zheng, G. Theocharis, V. Tournat, V. Gusev, Quasi Topological Rotational Edge Waves in Mechanical Granular Graphene, **PRB 97, 060101(R) (2018)**